

## **Calculation Policy**

## About our calculation policy

The following calculation policy has been devised to meet requirements of the National Curriculum for the teaching and learning of mathematics, and is also designed to give pupils a consistent and smooth progression of learning in calculations across the school.

This calculation policy is focused on developing proficiency with the expected formal written methods by the end of year 6 and hence the progression guidance provided for each operation is designed to flow into the expected method as exemplified on the National Curriculum Appendix document, White Rose Maths and NCETM.

### Age-related expectations

The calculation policy is organised according to age stage expectations as set out in the National Curriculum, however it is vital that pupils are taught according to the stage that they are currently working at, being moved onto the next level as soon as they are ready, or working at a lower stage until they are secure enough to move on. It is expected that academies will work towards the fluency goals for each age group but that, where necessary, teachers will use approaches and materials from earlier year groups to bridge any gaps in a child's understanding.

Teachers should have an understanding of the expectations and progression for all year groups, regardless of which year group they teach.

## Concrete, Pictorial and Abstract Approach

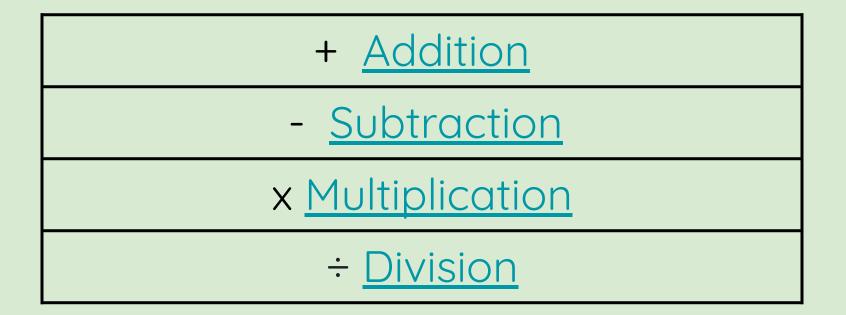
## Providing a context for calculation

It is important that any type of calculation is given a real life context or problem solving approach to help build children's understanding of the purpose of calculation, and to help them recognise when to use certain operations and methods when faced with problems. This must be a priority within calculation lessons.

## Teaching calculations using concrete materials

In order for children to develop a deep conceptual understanding of mathematics, we believe that teaching of calculations ought to be supported by the use of concrete materials. Children should be taught, and encouraged to use, manipulatives, pictorial representations and symbolic representations cyclically throughout all key stages. Specific practical equipment and approaches have been suggested for each age group to support children in developing the conceptual understanding that will enable them to move more rapidly and efficiently towards the formal written methods expected. It is recommended that teachers encourage children to simultaneously carry out the calculation practically using the equipment/representation suggested <u>and</u> to record this calculation step by step using the parallel formal written method.

## **Table of Contents**



## Addition

Year 1		
Objectiv	<b>/e:</b> to add 1 and 2-digit numbe	ers to 20
Concrete	Pictorial	Abstract
Numicon, tens frames and bead strings.	Bar models, part-whole models and number lines.	8 + 7 = 15 2 5

Year 2		
Obje	ctive: to add three 1-digit num	nbers
Concrete	Pictorial	Abstract
Numicon and tens frames. $ \begin{array}{c}  \end{array} $	Bar models and part-whole models. $ \begin{array}{c}                                     $	7 + 6 + 3 = 16 7 + 6 + 3 = 16 10

Year 2/3		
Objective:	to add 1-digit and 2-digit num	bers to 100
Concrete	Pictorial	Abstract
Place value counters	Bar models, number lines, hundred squares and part-whole models. $ \begin{array}{c}             2 \\             38 \\             \hline      \hline      \hline          $	<b>38 + 5 = 43</b>

Year 2/3			
Objec	Objective: to add 2-digit numbers to 100		
Concrete	Pictorial	Abstract	
Place value counters and base ten.	Bar models, number lines and part-whole models.	38 + 23 = 61 38 + 23	
Tens Ones	38 40 61	<u>61</u> 1	

Year 3			
Objectiv	<b>Objective:</b> to add numbers with up to 3 digits		
Concrete	Pictorial	Abstract	
Place value counters and base ten.	Bar models and part-whole models.		
	265 (265) (164) (265) 164 (265) (164)	265 + 164 = 429 $265 + 164$ $429$ 1	

Year 4		
Objectiv	<b>ve:</b> to add numbers with up to	o 4 digits
Concrete	Pictorial	Abstract
<image/>	Bar models and part-whole models. $ \begin{array}{r} 1,378 \\ 2,148 \\ \hline 2,138 \\ \hline 1,378 \\ \hline 2,138 \\ \hline 2,138 \\ \hline 1,378 \\ \hline 1,378 \\ \hline \end{array} $	$1 3 7 8 \\ + 2 1 4 8 \\ 3 5 2 6 \\ 1 1$ 1,378 + 2,148 = 3,526

Year 5/6		
Objective: to add numbers with more than 4 digits		
Concrete	Pictorial	Abstract
Place value counters.	Bar models and part-whole models.	
HTh TTh Th H T O	? 61,731	104,328 + 61,731 = 166,059
	104,328	1 0 4 3 2 8 + 6 1 7 3 1
	61,731	1 6 6 0 5 9
	? [ 104,328 61,731	

Year 5		
Objective: to	o add numbers with up to 3 de	cimal places
Concrete	Pictorial	Abstract
<image/>	Bar models and part-whole models. 241   3.65   7   7   1   3.65   7   1   1   1   1   1   1   1   1   1	3.65 + 2.41 = 6.06 $3.65 + 2.41$ $6.06$ $1$

## Subtraction

Year 1		
Objectiv	<b>e:</b> to subtract 1-digit numbers	within 10
Concrete	Pictorial	Abstract
Numicon, cubes, tens frames and bead strings.	Bar models, part-whole models and number lines.	<b>7 - 3 = 4</b>

Year 1/2		
Objective	to subtract 1 and 2-digit num	bers to 20
Concrete	Pictorial	Abstract
Numicon and tens frames .	Bar models, part-whole models and number lines.	14 - 6 = 8

Year 2/3			
Objective:	Objective: to subtract 1 and 2-digit numbers to 100		
Concrete	Pictorial	Abstract	
Place value counters and base ten.	Bar models, part-whole models and number lines.		
Tens     Ones       O     O     O       O     O     O       O     O     O       O     O     O       O     O     O       O     O     O       O     O     O       O     O     O	65 28	65 - 28 = 37 $^{5}_{65}$	
Tens     Ones       Image: Construction of the second secon	65 L ? 28	<u>- 28</u> <u>37</u>	
	+2 $+30$ $+528 30 60 65$		

Year 3			
Objective	Objective: to subtract numbers with up to 3 digits		
Concrete	Pictorial	Abstract	
	Bar models, part-whole models and number lines. 65 $65$ $28$ $65$ $28$ $42$ $42$ $43$ $43$ $43$ $44$	$435 - 273 = 162$ $\begin{array}{r} {}^{3}4 \\ - 273 \\ - 273 \\ 162 \end{array}$	

Year 4		
Objective	to subtract numbers with up	o to 4 digits
Concrete	Pictorial	Abstract
Place value counters and base ten.         Image: Hundreds Tens Ones         Image: Hundreds Tens Ones<	Bar models and part-whole models. 4,357 2,735 ? 4,357 2,735 ? 4,357 ? 4,357 ? 4,357 ? 4,357 ? 7	4,357 - 2,735 = 1,622 $4,357 - 2,735 = 1,622$ $- 2735$ $- 2735$ $1622$

	Year 5/6	
Objective: to	subtract numbers with more	than 4 digits
Concrete	Pictorial	Abstract
Place value counters.	Bar models and part-whole models. $ \begin{array}{r} 294,382 \\ \hline 182,501 \\ \hline 294,382 \\ 2$	$294,382 - 182,501 = 111,881$ $2 9 \frac{3}{13} \frac{1}{3} \frac{8}{2} \frac{2}{-1} \frac{1}{8} \frac{2}{2} \frac{5}{5} \frac{0}{1} \frac{1}{1} \frac{1}{1} \frac{1}{8} \frac{8}{8} \frac{1}{1}$

Year 5/6		
Objective: to s	ubtract numbers with up to 3	decimal places
Concrete	Pictorial	Abstract
<image/>	Bar models and part-whole models. $\begin{array}{c} 27 & 7 \\ \hline 27 & 7 \\ \hline 543 \\ \hline 2.7 & 7 \end{array}$	$5.43 - 2.7 = 2.73$ $\begin{array}{r}4 & 1 \\ \cancel{5}.43 \\ - 2.7 \\ 2.73 \end{array}$

# Multiplication

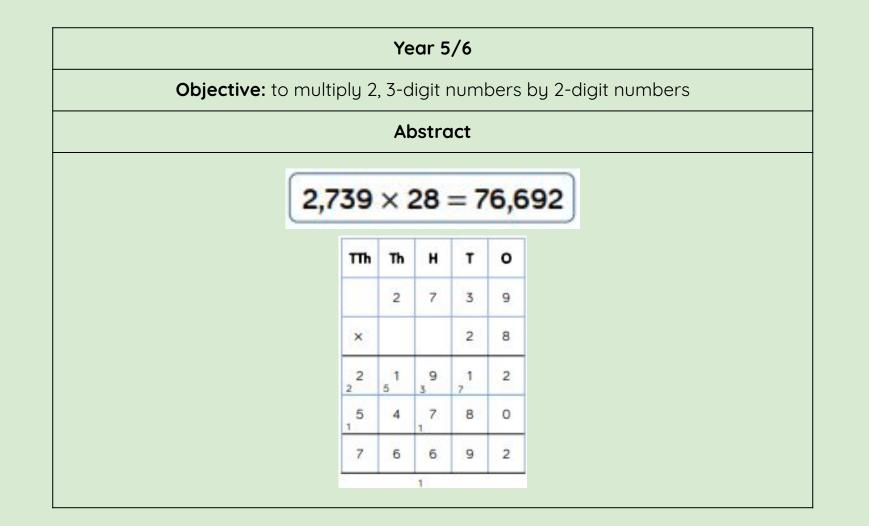
Year 1/2			
<b>Objective:</b> to	Objective: to solve 1-step problems using multiplication		
Concrete	Pictorial	Abstract	
Numicon, cubes, tens frames and bead strings.	Arrays and number lines.		
		5+5+5+5=20 $4 \times 5 = 20$ $5 \times 4 = 20$	
-00000-00000-00000-00000-			

	Year 3/4	
Objective: to m	nultiply 2-digit numbers by 1-	digit numbers
Concrete	Pictorial	Abstract
Place value counters and base ten.	Place value chart.	<b>34</b> × <b>5</b> = 170
		H T O 3.4 × 5 2 0 (5×4) + 1 5 0 (5×30)
		3 7 0
		нто
		x 5
		1 7 0
		1 2

	Year 4	
Objective: to	multiply 3-digit numbers by 1-c	digit numbers
Concrete	Pictorial	Abstract
Place value counters and base ten.	Place value chart.	<b>245</b> × 4 = 980
		H T O
		× 4
Hundreds Tens Ones		980

	Year 5	
Objective: to	multiply 4-digit numbers by 1-	digit numbers
Concrete	Pictorial	Abstract
Place value counters.	Place value chart.	
		1,826 × 3 = 5,478
		Th H T O 1 8 2 6
		× 3
		2 1

	Year 5	
Objective: to n	nultiply 2, 3-digit numbers by	2-digit numbers
Concrete	Pictorial	Abstract
Place value counters.	Place value chart.	$22 \times 31 = 682$ $\boxed{ \times 20 2 \\ 30 600 60 \\ 1 20 2 }$ $\boxed{ H T 0 \\ 2 2 \\ \times 3 1 \\ 2 2 2 \\ 6 6 0 \\ 6 8 2 }$ $234 \times 32 = 7,488$
		Th H T O
		x 3 2
		4 6 8
		17 10 2 0
		7 4 8 8



## Division

Year 1/2			
Objective: to solv	<b>Objective:</b> to solve 1-step problems using multiplication (sharing)		
Concrete	Pictorial	Abstract	
Counters.	Bar models, arrays and grouping.	20 ÷ 5 = 4	

Year 1/2			
Objective: to solve	<b>Objective:</b> to solve 1-step problems using multiplication (grouping)		
Concrete	Pictorial	Abstract	
Counters, bead strings and tens frames.	<image/>	20 ÷ 5 = 4	

	Year 3 Objective: to solve 1-step problems using multiplication (grouping)		
Objective: to solve			
Concrete	Pictorial	Abstract	
Counters and base ten.Image: colspan="2">Image: colspan="2"Image: colspan="2" </td <td>Place value chart and part-whole model.</td> <td><b>48 ÷ 2 = 24</b></td>	Place value chart and part-whole model.	<b>48 ÷ 2 = 24</b>	

	Year 3/4	
Objective: to div	vide 2-digits by 1-digit (sharing	g with exchange)
Concrete	Pictorial	Abstract
Image: Counters and base ten.         Image: Counters and base ten. </td <td>Place value chart, bar model and part-whole model. <math>33^{\circ}</math> <math>333335</math> <math>\overline{)}</math> <math>\overline{)}</math> <math>\overline</math></td> <td>52 ÷ 4 = 13</td>	Place value chart, bar model and part-whole model. $33^{\circ}$ $333335$ $\overline{)}$ $\overline{)}$ $\overline$	52 ÷ 4 = 13

	Year 3/4	
Objective: to divi	ide 2-digits by 1-digit (sharing	with remainders)
Concrete	Pictorial	Abstract
Counters and base ten.Image: Counters	Place value chart, bar model and part-whole model. 6000000000000000000000000000000000000	53 ÷ 4 = 13 r1

	Year 4	
Objectiv	<b>e:</b> to divide 3-digits by 1-digit	(sharing)
Concrete	Pictorial	Abstract
H       T       O         O       O       O         O       O       O         O       O       O         O       O       O	Place value chart, bar model and part-whole model.	844 ÷ 4 = 211

	Year 5	
Objective	e: to divide 2-digits by 1-digit (	grouping)
Concrete	Pictorial	Abstract
Tens       Ones         Image: Ima	Place value chart	<b>52</b> ÷ <b>4</b> = <b>13</b> $1  3  4  5  12$

	Year 5	
Objective	e: to divide 3-digits by 1-digit (	grouping)
Concrete	Objective: to divide 3-digits by 1-digit (grouping)         Concrete       Pictorial       Abstract         Counters       Place value chart       856 ÷ 4 = 214	
		2 1 4

	Year 5	
Objective	e: to divide 4-digits by 1-digit (	grouping)
Concrete	Pictorial	Abstract
T       T	Place value chart	$8,532 \div 2 = 4,266$

Objective: to divide multi digits by 2-digits (short division)         Abstract $432 \div 12 = 36$ $\boxed{0 \ 3 \ 6}$ $12 \ 4 \ 43 \ 72$ $\boxed{12 \ 4 \ 43 \ 72}$ $7,335 \div 15 = 489$ $\boxed{0 \ 4 \ 8 \ 9}$ $15 \ 30 \ 45 \ 60 \ 75 \ 90 \ 105 \ 120 \ 135 \ 150$		•	Year	5					
432 ÷ 12 = 36       0       3       6         12       4       3       7         12       4       4       3       7         7,335 ÷ 15 = 489       15       7       7       13       13	Objective: to div	ide multi	digits	by 2	2-diç	gits (	shor	t divis	ion)
$432 \div 12 = 36$ 12       4       4       3       7         12       4       4       3       7         7,335 ÷ 15 = 489       15       7       7       13       13		A	bstra	ct					
12       4       3       7         12       4       4       3       7         7,335 ÷ 15 = 489       15       7       7       13       13	<b>472</b> · 12 - 76		[			0	3	6	
$7,335 \div 15 = 489$	432 ÷ 12 = 30				12	4	4 3	7 2	
$7,335 \div 15 = 489$									
$7,335 \div 15 = 489$			1						
	7,335 ÷ 15 = 489		Abstract $12$ $0$ $3$ $6$ $12$ $4$ $3$ $7$ $12$ $4$ $4$ $7$ $12$ $4$ $4$ $7$ $12$ $4$ $8$ $9$ $15$ $7$ $7$ $13$ $13$						
15         30         45         60         75         90         105         120         135         150				15	7	3	3	5	
	15 30 45	60 75	90	105	120	135	150		
							1	_	

Year 6							
<b>Objective:</b> to divide multi digits by 2	-digits (long divi	sion	)				
Abstract							
<ol> <li>Write down the multiples</li> <li>Divide</li> <li>Multiply</li> <li>Subtract</li> <li>Bring the number down</li> <li>Repeat</li> </ol>	$12 \times 1 = 12$ $12 \times 2 = 24$ $12 \times 3 = 36$ $12 \times 4 = 48$ $12 \times 5 = 60$ $12 \times 6 = 72$ $12 \times 7 = 84$ $12 \times 8 = 96$ $12 \times 7 = 108$ $12 \times 10 = 120$	1	2 -	043	3 3 6 7 7	6 2 2 2 0	(×30) (×6)

		Year 6								
	Objective: to divide multi	digits by 2-digits (long	division with	ar	en	nai	nd	er)	)	
		Abstract								
			1 × 15 = 15				24	t r	1	2
1.	Write down the multiples	372 ÷ 15 = 24 r12	2 × 15 = 30 3 × 15 = 45	1	5		7 2	2		
2.	Divide		$4 \times 15 = 60$	-	-	3	0 0	)	1	1
3.	Multiply		5 × 15 = 75				7 2	2	1	
1.	Subtract		$10 \times 15 = 150$		-		6 (	)	t	1
5. 6	Bring the number down						1 2	2		
5.	Repeat		1 × 15 = 15							
		$372 \div 15 = 24 \frac{4}{5}$	$2 \times 15 = 30$				2	4	4	
		012 10 - 245	$3 \times 15 = 45$	1	5	3	7	2	. 3	
			$4 \times 15 = 60$		-	3	0	0		
			5 × 15 = 75				7	2	13	
			$10 \times 15 = 150$		_		6	0		
					-		1	2		